17.74. Model: The air is assumed to be an ideal gas. Because the air is compressed without time to exchange heat with its surroundings, the compression is an adiabatic process.

Solve: The initial pressure of air in the mountains behind Los Angeles is $p_i = 60 \times 10^3$ Pa at $T_i = 273$ K. The pressure of this air when it is carried down to the elevation near sea level is $p_f = 100 \times 10^3$ Pa. The adiabatic compression of a gas leads to an increase in temperature according to Equation 17.39 and Equation 17.40, which are

1

$$T_{\rm f}V_{\rm f}^{\gamma-1} = T_{\rm i}V_{\rm i}^{\gamma-1} \Longrightarrow \left(\frac{T_{\rm f}}{T_{\rm i}}\right) = \left(\frac{V_{\rm i}}{V_{\rm f}}\right)^{\gamma-1} \qquad p_{\rm f}V_{\rm f}^{\gamma} = p_{\rm i}V_{\rm i}^{\gamma} \Longrightarrow \left(\frac{p_{\rm f}}{p_{\rm i}}\right)^{\frac{1}{\gamma}} = \frac{V_{\rm i}}{V_{\rm f}}$$

Combining these two equations,

$$\left(T_{\rm f}/T_{\rm i}\right) = \left(p_{\rm f}/p_{\rm i}\right)^{\frac{\gamma-1}{\gamma}} \Rightarrow T_{\rm f} = T_{\rm i} \left(\frac{100 \times 10^3 \text{ Pa}}{60 \times 10^3 \text{ Pa}}\right)^{\frac{1.4-1}{1.4}} = (273 \text{ K}) \left(\frac{5}{3}\right)^{0.286} = 316 \text{ K} = 43^{\circ}\text{C} = 109^{\circ}\text{F}$$